

5 METHOD FOR MONITORING WOOD-DRYING KILN
STATE

Technical Field

The invention relates to control systems for kilns used to dry wood.

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Background

Wood naturally contains moisture. However, for wood lumber to be useful for building, the moisture content must fall within certain constraints. Too much or too little water in the lumber can cause serious problems in the subsequent processing and use of the lumber, including warping or difficulties with painting or gluing. In order to provide a useful product, most lumber mills dry their lumber under controlled processes, such as in a kiln, prior to sale. It is difficult, however, to ensure that every board in a given charge will have exactly the same moisture content after drying.

Part of the problem lies in the nature of the wood itself; wood is a non-homogenous material that does not dry at a constant rate. Even within a charge with all boards of the same size and same type of wood there are many factors that can affect drying rate. Individual different boards may have natural variability in their drying rate, may start out with different moisture content, may be composed of different percentages of sapwood and hardwood, or may contain wet pockets. Moisture variations can also result from variable drying conditions between different kilns at the same mill or within a single kiln charge due to the locations of particular boards within a kiln. While the variation between charges or kilns can be monitored using averages, the variability within a charge is best monitored using standard deviations. One method by which this monitoring can be done is by using statistical process control (SPC).

SPC works to continuously improve the quality of a process through the constant application of statistical methods to data produced at various stages of the process.

5 Ideally, disturbances within the process are quickly discerned, then, using the data set, causes are assigned to those disturbances. In the best case, this is done with sufficient speed that investigation of the problem, diagnosis, and corrective action can be taken before many nonconforming products reach the final state of the process. This is usually done through the use of parametric control charts for variables. Generally, by plotting the
10 average and standard deviation of multiple samples on a control chart and comparing those values against computed acceptable limits, the chart can be used to determine if a process is going out of control.

The starting point for SPC analysis is an understanding of the underlying distribution of the data under analysis. The conventional assumption has been that wood moisture content data is approximately Normally distributed. However, wood is a non-homogenous material, and even when it is kiln-dried under controlled conditions, the moisture content retains large variability through the wood pieces, so a board with an acceptable average rating may be quite dry in one section and quite wet in another.
15 Additionally, because kiln-dried wood cannot be dried past the point at which it reaches equilibrium with the air in the kiln, there is an effective lower limit on moisture content. Thus, a Normal distribution has proven less than ideal for SPC analysis of wood drying and has made the task of creating a proper model for SPC analysis of wood drying difficult. It is desirable to design control charts specifically to monitor wood-drying, using a better-performing distribution model, if possible.
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25 The theory of variability is the basis for the construction and use of control charts. The purpose of any monitoring process is to sort out meaningful signals from background noise. A certain amount of variability in the moisture content of the dried lumber—background noise—exists in the kiln-drying process. Boards dry at different rates due to inherent properties in the wood itself, as mentioned above. This natural variability can be considered a system of “common causes.” A drying process that is operating with only common causes of variation is considered to be in statistical control.
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A major objective of the control charts is to sort out a meaningful signal from the background noise. When the moisture variability of the dried wood exceeds the background noise variability, this might indicate that there are problems associated with

5 the kiln itself. This variability in moisture content usually arises from three sources: improperly adjusted kiln equipment, operator errors, or defective raw material. Such variability may be large when compared to the background noise, and it usually represents an unacceptable level of process performance. These sources of variability are called "assignable causes." A process that is operating in the presence of such causes is
10 said to be "out of control." A kiln can operate in the "in control" state for a long time, producing acceptable moisture content levels in lumber. Eventually, however, assignable causes will occur, resulting in a shift to an out of control state, where the lumber produced no longer conforms to requirements.

A major objective of the control charts is to quickly detect the occurrences, or the
15 trends toward assignable causes of process shifts, which allows investigation into causes, and corrective action to be undertaken before many nonconforming units are produced. Control charts can also be used to estimate the parameters of the kiln-drying process, to determine process capability, and to incrementally improve the process. In general, control charts are an effective tool that can be used to reduce process variability.

20 Many quality control methods suggested in the literature are concerned with the average moisture content alone, and therefore use methods such as sample estimation, or go/no go decision criteria, such as acceptance sampling. Other methods have been tried that do concern themselves with variation, but are based on the assumption that moisture content has a Normal probability distribution. This assumption tends to erroneously
25 consider certain in-control conditions as defects or out-of-control conditions.

Furthermore, assumptions of Normality underlie many other common statistics, such as correlation coefficients, t-tests, and others that may be used in standard statistical analysis. The failure to understand that a distribution is not Normal leads to a rippling
30 statistical effect, with invalid assumptions producing incorrect answers which are themselves imperfectly analyzed, and so on.

Lognormal, rather than Normal, probability plotting for kiln analysis has been proposed by "Moisture Control During Kiln Drying," McMahon, 1961, in conjunction with frequency distribution analysis and quality control methods. These techniques were used to estimate the average moisture content and the percentage of moisture content

5 outside of certain boundaries. McMahon's methods were only approximate, however and introduced procedural errors that were potentially large. Additionally, McMahon's technique failed to properly account for the lower moisture content limit of kiln-dried wood. What is needed is a method that accounts for the lower moisture content limit that kiln-dried wood approaches and monitors kiln conditions more closely.

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Summary

A method for monitoring the drying of wood in a kiln is described herein. The method uses a set of known good samples of moisture content data for wood dried in a kiln to estimate a Lognormal statistical distribution which approximates the known good 15 set of data. The method estimates three parameters of a Lognormal distribution: the threshold parameter, the shape parameter, and the scale parameter. Then one or more new sample of moisture content data is obtained from a subsequent drying in the kiln. The method develops one or more control charts containing center lines and control limits which monitor at least one of the estimated parameters. Next, data from the new 20 sample or samples of moisture content data is transformed to represent the parameters on the control charts. Finally, a determination is made about whether the kiln is operating in an in-control or out-of-control state.

A computer-readable medium is also described herein. The computer-readable medium contains instructions which, when executed, obtain a known good set of samples 25 of moisture content data from wood dried in a kiln. Then the instructions use the known good data set to estimate parameters for a Lognormal distribution which approximates the known good data. Next the instructions obtain new moisture data for wood dried in the kiln. The instructions then create control charts based on the estimated Lognormal parameters, transform the new data to be represented on the control charts, and determine 30 whether the kiln is operating in an out-of-control state.

Additional features and advantages of the invention will be made apparent from the following detailed description of embodiments that proceeds with reference to the accompanying drawings.

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Brief Description Of The Drawings

Figure 1 is a diagram of a suitable environment in which described embodiments may be implemented.

10 Figure 2 is a diagram of a suitable environment for measuring moisture content of wood.

Figure 3 is a diagram showing examples of wood moisture content distribution patterns.

Figure 4 is a diagram showing examples of different distribution models.

Figure 5 is a block diagram of a method to develop control charts

15 Figure 6 is a block diagram of a method to estimate Lognormal shape and scale parameters.

Figure 7 is a block diagram of a method to create a control chart.

Figure 8 is a block diagram of a method to sample, transform and plot sample data to determine if a kiln is out of control.

20 Figure 9 is a diagram showing examples of control charts produced from a Lognormal distribution model.

Detailed Description

The following description is directed to improvements in creating quality control charts so that they more accurately and realistically monitor the variability of moisture content in kiln-dried lumber. These control charts are then used with more-recently collected data to determine if a kiln is out-of-control.

1. Moisture Content Measuring Environments

In an exemplary embodiment, moisture control measurements are collected from 30 kiln-dried lumber. Figure 1 depicts one environment for measuring moisture content in wood. In the illustrated embodiment, a lineal moisture content sensor 102 is controlled

5 by a moisture content control console 104. By adjusting various settings on the console 104, the sensor 102 can be made to measure the moisture content of various types, sizes, and shapes of wood. When data is received by the console 104, the data is sent to a computer 106, running moisture content monitoring software 108 (not pictured). As will be discussed below, the data received by the computer 106 can be analyzed by software 108 to determine if any out-of-control situations exist in the drying process.

10 With respect to Figure 2, an environment featuring various moisture sensors in a lumber mill is shown. In the illustrated embodiment, wood boards 201, which have been dried in a kiln, are sent through various in-line continuous moisture sensors, including a lineal moisture sensor 204 and a transverse moisture sensor 206, both controlled by 15 moisture control consoles 202. Also illustrated is computer 208, running moisture content analysis software 210, which collects data from the moisture content control consoles 202 for analysis. In another embodiment, moisture content readings may be made by types of sensors other than those illustrated, including a hand-held sensor, a pin-type sensor, or a contact sensor. In yet another embodiment the computer 208 and 20 software 210 may be integrated into individual control consoles 202 or the system may incorporate a single master computer which communicates with every control console and sensor to receive and analyze moisture content data.

2. Particulars of Wood Moisture Content Analysis and Lognormal Distribution

25 As was mentioned above, the unique nature of wood makes it difficult to dry every board in a kiln charge to the same moisture content, providing a variation. Even when boards are made of the same type of wood, are cut to the same specifications, and are dried for identical times and at identical temperatures, variations can still occur between kilns, between charges within a kiln, between boards in a single charge, and 30 even within a single board. Thus, in order to provide as accurate a measure as possible of the stability and consistency of the drying process, statistical methods can be used. However, because the data concerns moisture content in wood, additional consideration must be given to the statistical model used to analyze the data.

5 Figures 3a-d illustrate various examples of distribution for various samples of wood moisture content data. The examples shown were produced by the inventors from studies done by Pratt in 1953, McMahon in 1961, Bassett in 1969, and Milota and Wu in 1995. For ease of description, relevant aspects of the moisture content data distribution examples will be discussed with reference to the histogram displayed in Figure 3d.

10 Of chief concern for statistical modeling are the finite left end and positive skewness of the distribution. As the example histogram of Figure 3d demonstrates, and as the histograms of the other figures support, there is a tendency for moisture content distribution to drop off dramatically on the left end of the distribution. This is illustrated in Figure 3d by the location 304. Typically, this dramatic drop-off is due to the fact that
15 the wood cannot have a moisture content lower than the equilibrium moisture content (EMC) set up in the air of the kiln during the drying process, and in any case can never have a moisture content lower than zero. Thus there is a physical lower-bound to the moisture content that can be achieved by kiln-drying, and so a lower-bound to any moisture-content data that can be measured. Additionally, because not every piece of
20 wood dries at the same rate, moisture content data from kiln-dried wood exhibits a positive skewness, as demonstrated by the region 306. This means moisture content data distributions tend to show a trailing right-hand side even while the left had side has a definite edge. While the illustrated characteristics of moisture content data distribution are not necessarily found in every sample of dried wood, they are common to most
25 samples taken, and are thus important to consider when searching for a model that fits well. The system and methods described herein account for these features through the use of a 3-parameter Lognormal distribution model.

Figures 4a and 4b illustrate examples of Normal and Lognormal distribution models. In the example graph of Figure 4a a Normal distribution curve is demonstrated.
30 As the graph of Figure 4a demonstrates, Normal distribution curves are horizontally symmetrical and are positively and negatively unbounded. Thus, the Normal curve is frequently not the best fit for the types of distributions mentioned above with respect to Figures 3a-d.

5 Lognormal distribution models, however, do exhibit some of the characteristics described above. A Lognormal distribution model describes a variable that is distributed so that the natural logarithm of the variable has a Normal distribution. The graph of Figure 4b illustrates a sample Lognormal distribution curve. Unlike the Normal distribution curve in Figure 4a, the Lognormal curve demonstrates a positive skewness
10 similar to that described in region 306 of Figure 3d. The Lognormal distribution curve of Figure 4b also demonstrates a left-hand drop-off similar to that illustrated in location 304 of Figure 3d. In fact, as will be described below, the Lognormal distribution utilized in the present system includes a threshold parameter which provides a bounded minimum to the distribution, thus more closely approximating the behavior of kiln-dried wood.

15 The Lognormal distribution model utilized in the present system and method makes use of three parameters, a threshold parameter θ , a scale parameter μ , and a shape parameter σ . As described above, the use of the threshold parameter is to provide a lower bound for the distribution model, i.e. a minimum amount of water that could exist under the drying conditions being studied. The scale parameter essentially serves to stretch or
20 compress the curve on the horizontal axis, while the value of the shape parameter subtly affects the shape of the curve. The use of parameters such as these is well understood in general statistical distribution analysis, although not with regard to analysis of wood moisture content. Mathematically, the general form of this Lognormal probability distribution function with three parameters is given by the function:

$$25 f(x) = \frac{e^{-(\ln(x-\theta)-\mu)^2/(2\sigma^2)}}{(x-\theta)\sigma\sqrt{2\pi}} \text{ for } x \geq \theta \quad (1)$$

While data that follows a Lognormal distribution can be described with the function (1), the moisture content data is not analyzed directly in the system and methods described herein. Traditionally, a control chart plots the arithmetic mean and standard deviation (or variance) of multiple samples against a central tendency line and control
30 limits in order to monitor process conditions. However, for variables that follow a Lognormal distribution, the distribution of standard deviations is not well understood. Additionally, because of the nature of Lognormal distributed variables, the arithmetic

5 mean of a sample is not as good an indicator of central tendency as the geometric mean. Thus, monitoring of averages and standard deviations of the direct sample data is not as useful as other methods.

Instead, the present methods and system perform analysis on logarithmically-transformed data in order to monitor the shape and scale parameters themselves. Because 10 the logarithm of a Lognormal variable is itself Normally distributed, it is known that for a variable X which is distributed Lognormal with a threshold parameter θ , a scale parameter μ , and a shape parameter σ , then the logarithmically-transformed variable $Y = \ln(X - \theta)$ has a normal distribution with mean μ and standard deviation σ . Because methods of SPC are well known for Normal variables, techniques for monitoring 15 the mean and standard deviation of the logarithmically-transformed variable will provide information about changes in the shape and scale parameters of the Lognormal distribution. It is the monitoring of these parameters that the techniques below focus on.

3. Creation of Control Charts for Wood Moisture Content Data

Figure 5 illustrates a block diagram which describes, in one embodiment, a process for creating a control chart for wood moisture content data. Starting at block 20 502, known good data is collected so that proper limits and a center line for the control charts can be developed from the data. Because differences in wood type or kiln can affect the drying process, in the preferred embodiment the collection of known good data is done for the specific kiln and under the same conditions in which subsequent drying 25 will take place. In one embodiment this is done by taking multiple samples, with each sample containing multiple wood moisture content readings. These conditions can include, in various embodiments: the species of wood, the type of lumber made of the wood, the method of stacking wood in the kiln, and the drying schedule. In one embodiment the data is divided up for analysis into subgroups, allowing greater discernment of kiln drying problems. Thus, analysis can be performed at once for all 30 boards in a kiln charge, between packs of boards in a kiln charge, or even between boards in a particular pack. This provides flexibility to more readily identify and correct problems.

5 In one embodiment, in order that the data can be trusted to properly represent moisture content data distribution, the data collection is done at a time when the kiln being used is known to be "in-control," i.e. operating within normal parameters and producing conforming product. In the preferred embodiment, care is taken during the process of block 502 to ensure that the known good data taken is done randomly and
10 independently. In one embodiment this is done through a random sampling with replacement, and by ensuring that no two measurements had any overlap.

Next, at block 504, it is determined if the known good data fits a Lognormal distribution. In the preferred embodiment the process of block 504 is performed so that in case, for some particular set of conditions, the data does not follow a Lognormal
15 distribution, subsequent analysis can follow Normal (or other) distribution techniques rather than the Lognormal techniques described herein. In various embodiments, this determination is performed through the use of graphical and/or numerical methods, such as investigation of symmetry and probability plotting of the Lognormal variable X and goodness-of-fit tests of the Normal distribution to the transformed variable Y .

20 If, at block 504 it is determined that the known good data follows a Lognormal distribution, then at block 508 a Lognormal distribution is estimated that approximates the known good data. In the preferred embodiment, the threshold parameter θ is first approximated from the sample at block 510, and then approximate values for the scale parameter μ and the shape parameter σ can then be calculated from θ at blocks 512 and
25 514, respectively.

With respect to the process of block 510, the threshold parameter in the illustrated embodiment is estimated from the known good data set in order that the other parameters can be calculated. While typically the EMC of the kiln during drying is known, that value is not substituted for the threshold in the preferred embodiment. This is because, in
30 order to quickly pull water out of wood, the wood is never allowed to reach the EMC of the kiln before the EMC is changed. Thus, in the illustrated embodiment, it is not assumed that the EMC is the threshold of the distribution.

5 In one embodiment, this is done through the technique of using local maximum likelihood estimators for θ , as will be understood. In one embodiment, a local maximum likelihood estimator for θ , using an ascending ordered sample x_1, x_2, K, x_n , is given by:

$$F(\theta) = \left[\sum_i^n \left(\frac{1}{x_i - \theta} \right) \right] * \left[n * \sum_i^n \ln(x_i - \theta) - n * \sum_i^n \ln^2(x_i - \theta) + \left(\sum_i^n \ln(x_i - \theta) \right)^2 \right] - n^2 * \sum_i^n \left(\frac{\ln(x_i - \theta)}{x_i - \theta} \right) = 0 \quad (2)$$

This equation can then be solved using trial and error with linear interpolation to
10 yield an estimator for the threshold parameter, $\hat{\theta}$. In other embodiments, when this technique does not yield a valid result, an alternative technique using modified moment estimators, as demonstrated in "Modified Moment Estimation for the Three-Parameter Lognormal Distribution," Cohen et al., 1985. Once a sufficient estimate for θ is found, estimates for the other two parameters can be found by:

$$15 \quad \hat{\mu} = \frac{1}{n} * \sum_i^n \ln(x_i - \hat{\theta}) \quad (3)$$

$$\hat{\sigma}^2 = \frac{1}{n} * \sum_i^n \ln^2(x_i - \hat{\theta}) - \left[\frac{1}{n} * \sum_i^n \ln(x_i - \hat{\theta}) \right]^2 \quad (4)$$

Relations (2), (3) and (4) come from "Estimating Parameters of Logarithmic-Normal Distributions by Maximum Likelihood," A.C. Cohen, 1951. After calculation of the Lognormal parameters, the process at block 516 creates one or more control charts.
20 As was explained above, control charts can measure either the scale parameter, as in blocks 518 and 522, or the shape parameter, as in blocks 520 and 522. In the preferred embodiment, the shape and scale parameters are monitored, as values for them can be determined from the threshold parameter. While creating a control chart that directly monitors threshold is more difficult, changes in the threshold parameter in one embodiment can be observed when changes occur in either the shape or scale parameter without a corresponding change in the other. As will be discussed below with respect to Figure 7, control charts may be created in either a logarithmic scale or in an "antilog" scale, which is the same scale in which the original moisture content data was taken.

5 Figure 6 illustrates a block diagram which describes, in one embodiment, the process of calculating estimates for μ and σ . This process can be performed as the process of blocks 512 and 514 of Figure 5. Ristea and Maness, 2001, demonstrates that this process is equivalent to performing the calculations given above in (3) and (4). The illustrated embodiment assumes that the known good data set comprises m samples with 10 each sample comprising n moisture content measurements. In a preferred embodiment, m is at least 20, while n is 5 or greater. At block 602, each sample x_1, x_2, K, x_n is transformed to normality by first subtracting the estimated threshold parameter and then taking the natural logarithm, giving a normalized sample y_1, y_2, K, y_n by the equation:

$$\ln(x_i - \hat{\theta}) = y_i \quad (5)$$

15 Next, at block 604, calculations are made for each of the m samples. In block 606, for each sample a mean normalized value, \bar{y} , is calculated by taking the mean of each of the normalized measurements:

$$\bar{y} = \frac{y_1 + y_2 + K + y_n}{n} \quad (6)$$

Similarly, in block 608, the standard deviation, S , of each sample is calculated. 20 Next, at block 610, the parameters μ and σ are calculated from the \bar{y} 's and S 's by taking the mean over every sample. Thus, if \bar{y}_i and S_i are the mean and standard deviation of the i^{th} sample, respectively, and there are m samples, then:

$$\bar{\bar{y}} = (\bar{y}_1 + \bar{y}_2 + K + \bar{y}_m)/m \quad (7)$$

$$\bar{S} = (S_1 + S_2 + K + S_m)/m \quad (8)$$

25 Because $\bar{\bar{y}}$ is an estimate of the population mean of the Normal variable, it is also an estimate of the scale parameter μ . Additionally, because of the way $\bar{\bar{y}}$ is created by mathematical manipulation of the logarithmically-normalized moisture content measurements, $\bar{\bar{y}}$ is in fact the geometric mean of those measurements, after taking threshold scaling into account. As mentioned above, the geometric mean is known to be 30 a better indicator of the central tendency of Lognormal distributed variables.

5 \bar{S} , however, is not an unbiased estimator of the Lognormal shape parameter. In
order to provide an unbiased estimate of σ , at block 616, in the preferred embodiment,
 \bar{S} is divided by a constant, c_4 , the value of which depends on the sample size. The values
of c_4 for different sized samples can be found in the literature. Thus, an estimate for σ is
provided by \bar{S} / c_4 in block 616 and the process of estimating the Lognormal parameters
10 is completed.

Figure 7 illustrates a block diagram of, in one embodiment, a process used to
create control charts for the scale and shape Lognormal parameters. Block 516 represents
the process of developing the charts themselves before new data is plotted on them.
Beginning with block 704, a sample size n is established for the all new data that will be
15 measured as part of the SPC process. The sample size must be established because the
control limits for the scale parameter are dependent on the sample size, as will be shown
below. Next, at block 706, the center lines of the control charts are chosen. The center
lines are simply $\hat{\mu}$ and $\hat{\sigma}$, as the control charts will be measuring changes in scale and
shape of the Lognormal distribution. Because the estimated $\hat{\mu}$ and $\hat{\sigma}$ parameters have
20 been calculated in the process illustrated in Figure 6, the center lines are already known
to be \bar{y} and \bar{S} / c_4 for the scale and shape control charts, respectively. Next, in block 708,
the control limits for each of the control charts are calculated.

For the scale chart, control limits are established in the traditional fashion for a
control chart of averages. Thus, in block 710, in one embodiment, conventional "3-
25 sigma" limits are established around the center line \bar{y} . The plotted data points will be
averages of the transformed measurement samples, i.e. \bar{y} . The sample means \bar{y} is
normally distributed and has standard deviation $\hat{\sigma} / \sqrt{n}$. Hence the Upper Center Line,
Center Line, and Lower Center Line of the control chart are:

$$\left\{ \begin{array}{l} UCL = \bar{y} + 3 * \frac{\bar{S}}{c_4 \sqrt{n}} \\ Center\ Line = \bar{y} \\ LCN = \bar{y} - 3 * \frac{\bar{S}}{c_4 \sqrt{n}} \end{array} \right. \quad (9)$$

5 For the shape chart, because the sample standard deviation is not normally distributed, 3-sigma limits cannot be used. However, it is known that the variance of a Normal variable such as Y is chi-square distributed. Thus, in one embodiment, at block 712 probability limits are used to calculate the control limits. In one embodiment, this is
10 done by the following calculations:

$$\left\{ \begin{array}{l} UCL = \frac{\bar{S}}{c_4} \sqrt{\frac{X^2_{\alpha/2,n-1}}{n-1}} \\ Center\ Line = \frac{\bar{S}}{c_4} \\ LCN = \frac{\bar{S}}{c_4} \sqrt{\frac{X^2_{1-\alpha/2,n-1}}{n-1}} \end{array} \right. \quad (10)$$

15 While the calculations given in (9) and (10) create control charts in one embodiment, because of the logarithmic transformation done on the data, the scale of the charts themselves has no units. Thus, it may not provide the detail of information desired
20 when monitoring the wood drying process. Thus, in one embodiment, at block 714, the limits and center line are scaled to be put back into the original scale of measurement. In one embodiment this is done by taking the antilog of the limits or center line through exponentiation and then, in the case of the scale parameter, adding back the estimated threshold. The threshold does not affect the standard deviation and so does not need to be added back for the shape parameter chart. Thus the calculations in (9) become, in scaled form:

5

$$\left\{ \begin{array}{l} UCL = \hat{\theta} + \exp\left(y + 3 * \frac{\bar{S}}{c_4 \sqrt{n}}\right) \\ Center\ Line = \hat{\theta} + \exp\left(\bar{y}\right) \\ LCN = \hat{\theta} + \exp\left(y - 3 * \frac{\bar{S}}{c_4 \sqrt{n}}\right) \end{array} \right. \quad (11)$$

and the calculations of (10) become:

$$\left\{ \begin{array}{l} UCL = \exp\left(\frac{\bar{S}}{c_4} \sqrt{\frac{X^2_{\alpha/2,n-1}}{n-1}}\right) \\ Center\ Line = \exp\left(\frac{\bar{S}}{c_4}\right) \\ LCN = \exp\left(\frac{\bar{S}}{c_4} \sqrt{\frac{X^2_{1-\alpha/2,n-1}}{n-1}}\right) \end{array} \right. \quad (12)$$

It will be demonstrated later that changing the scale in this manner does not qualitatively affect the general trends of the control charts, and thus the procedure of block 714 can be performed or not performed depending on the need of whoever or whatever is monitoring the control charts. Finally, at block 716, new data is plotted on the chart in order to monitor the drying process.

The process of block 716 is described in further detail with respect to Figure 8. Figure 8 shows, in one embodiment, the process of taking new data, transforming it, and plotting it on control charts so as to monitor the drying procedure. Starting at block 802, a new set of wood moisture content data is gathered. In a preferred embodiment, the gathering is done randomly and independently. In another preferred embodiment, the data is gathered from the same type of wood dried under the same conditions as that used to make the control charts. In yet another preferred embodiment, the new data is gathered in samples of the same size as was established at block 704. This is done to ensure that the proper calculations were performed for the control lines against which the new data will be measured. Continuing to block 808, the data is transformed so that it may be plotted on the chart. In block 810, each measurement is transformed from the original moisture content into a normalized logarithmic form, as was done for the known

- 5 good set of data in block 602. Next, the data is manipulated by sample so that it may be plotted. In block 814, the mean of each transformed sample in one embodiment is calculated if the chart being plotted on is a scale chart. This is done by taking the mean of all of the transformed values for a single sample, creating a \bar{y} value that can be plotted, similarly to the process described above in block 606. Thus, for each
- 10 sample x_1, x_2, K, x_n of size n , each plotted value \bar{y} is computed by:

$$\bar{y} = \frac{1}{n} * \sum_{i=1}^n \ln(x_i - \hat{\theta}) \quad (13)$$

- In block 816, in another embodiment the standard deviation of each sample of transformed data is calculated to determine an S value which can be plotted on a shape chart. Similarly to the discussion above with respect to Figure 7, the data determined now is unitless; if the same scale as the original moisture content data is desired, the calculated scaled antilog of the \bar{y} and S values must be found. Thus, in one embodiment, the \bar{y} and S values are changed to the original scale. This is done, similarly to above, by exponentiating the values, and, if the chart is a scale chart, adding the threshold parameter back in. For example, for the scale chart the value to be plotted can be
- 15 determined by:
- 20

$$\bar{y}_{\text{antilog}} = \hat{\theta} + \exp(\bar{y}_{\log}) \quad (14)$$

Because \bar{y} is the logarithmically-normalized mean of the original sample, \bar{y} is related to the geometric mean of the original sample measurements. Thus, in an alternate embodiment, the original-scale plot values can be found for a sample by:

25

$$\bar{y}_{\text{antilog}} = \hat{\theta} + \text{geomean}(x_i - \hat{\theta}) \quad (15)$$

Where *geomean* is the geometric mean. Thus (15) can be performed directly from the measurements by:

$$\bar{y}_{\text{antilog}} = \hat{\theta} + \left(\prod_{i=1}^n (x_i - \hat{\theta}) \right)^{\frac{1}{n}} \quad (16)$$

- Next, at block 820, the value is ready to be plotted on its control chart. Then, at
- 30 block 822 in one embodiment, it is determined if the kiln is in an out-of-control state. In

5 one embodiment determination that the kiln is out-of-control is done because a single
 \bar{y} or S value falls out side of the set control limits. In another, a minimum set number of
data points are required to fall outside the control limits before an out-of-control state is
assumed. In another, an out-of-control state may be inferred by the proximity of data
values to the control limits, regardless of whether and exceed the actual limits.

10 Figures 9a-d demonstrate examples of control charts for scale and shape, and
illustrate the similarities between unitless charts and charts in the original moisture
content units. In one embodiment these charts are displayed as new data is transformed
and compared to the control limits and center lines computed above. In another
embodiment the charts are not displayed, and other indications are made about the
15 relation between the transformed data and the control limits and center lines. The charts
of Figures 9a and 9b represent the same data for the scale parameter, with the chart of
Figure 9b having been transformed back into original unit scale. The charts of Figures 9a
and 9b are known as "y bar" and "antilog y bar" respectively. There is a symmetry shift
between the two charts; the chart of Figure 9a is symmetrical around its center line due to
20 the calculations in (9) while the chart in Figure 9b is asymmetrical due to the
exponentiation. However a graphical comparison between the two charts illustrates that
trends from sample to sample are similarly represented in both the unitless and original
scale charts. Similar tendencies can be observed in the unitless and original scale charts
for the shape parameter in Figures 9c and 9d. Thus, the act of scaling discussed above
25 with respect to Figures 7 and 8 is reasonable and in various embodiments can provide
similar monitoring abilities as the unitless charts.

The method described above provides an improved process for statistically
analyzing wood moisture content data in order to monitor drying kilns. The method
produces control charts which can be easily monitored, by computer or by human, in
30 order to determine if a given drying process is in-control. In view of the many possible
embodiments to which the principles of our invention may be applied, we claim as our
invention all such embodiments as may come within the scope and spirit of the following
claims and equivalents thereto.